

APPM 1345

Final Exam

Spring 2024

Name

Instructor

Lecture Section

This exam is worth 150 points and has 8 problems.

Make sure all of your work is written in the blank spaces provided. If your solutions do not fit, you may ask one of your proctors for a piece of scratch paper. Do NOT use any paper that you have brought with you.

Show all work and simplify your answers. Name any theorem that you use. Answers with no justification will receive no points unless the problem explicitly states otherwise.

Notes, papers, calculators, cell phones, and other electronic devices are not permitted

End of Exam Check List

1. If you finish the exam before 12:45 PM:

- Go to the designated area to scan and upload your exam to Gradescope.
- Verify that your exam has been correctly uploaded and all problems have been labeled.
- Leave the physical copy of the exam with your proctors in the correct pile for your Lecture Section.

2. If you finish the exam after 12:45 PM:

- Please wait in your seat until 1:00 PM.
- When instructed to do so, scan and upload your exam to Gradescope at your seat.
- Verify that your exam has been correctly uploaded and all problems have been labeled.
- Leave the physical copy of the exam with your proctors in the correct pile for your Lecture Section.

Formulas

$$\sin(2\theta) = 2 \sin \theta \cos \theta \quad \cos(2\theta) = 2 \cos^2 \theta - 1 = 1 - 2 \sin^2 \theta$$

$$\sum_{i=1}^n i = \frac{n(n+1)}{2} \quad \sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6} \quad \sum_{i=1}^n i^3 = \left(\frac{n(n+1)}{2}\right)^2$$

$$\int \frac{1}{\sqrt{1-x^2}} dx = \arcsin(x) + C \quad \int \frac{1}{1+x^2} dx = \arctan(x) + C$$

3. (16 points) Find the area of the largest rectangle which is symmetric around the y-axis, bounded below by the x-axis, and which has two corners touching the graph $f(x) = \frac{1}{1+x^2}$

4. (18 points) A bug moving in a straight line starts decelerating at time $t = 0$ at a constant rate $\frac{dv}{dt} = -5 \text{ m/s}^2$ for 5 seconds. Answer the following questions about the bug over the time interval $[0, 5]$.

(a)

8. (16 points) For each of the following questions, give a short justification for your answer.

(a) If $f(x)$ is an odd function and $\int_0^3 f(x) dx = 1$, find $\int_3^0 f(x) dx$.

(b) Find the absolute minimum of the function $f(x) = x - 2^x$, if it exists.

(c) Evaluate the limit $\lim_{h \rightarrow 0} \frac{\arctan(3x + 3h) - \arctan(3x)}{h}$:

(d) Suppose that $f(x)$ is differentiable everywhere, with $f'(1) = 1$ and $f(1) = 3$. Is there some value c such that $f'(c) = 1$?

END OF TEST

